

# Solar Irradiance Covariance Modeling for Oahu, Hawaii

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## Introduction

Solar irradiance measurements are highly correlated with the amount of energy produced by a grid of photovoltaic panels. Thus, reliable forecasting of irradiance will lead to reliable forecasting of energy output.

Utility-scaled solar plants are becoming more prominent. Modeling and forecasting methods of systems over various spatial and temporal resolutions are needed.

The spatio-temporal kriging forecaster [1]:

$$Z(s_0, t_0) = \mu(s_0, t_0) + \mathbf{c}(s_0, t_0)' \Sigma^{-1}(\mathbf{Z} - \mu)$$

where  $\mathbf{Z} = (Z(s_1, t_1), \dots, Z(s_n, t_n))'$  for  $n$  space-time coordinates,  $\mu = E[\mathbf{Z}]$ ,  $\Sigma = \text{cor}(\mathbf{Z})$ , and  $\mathbf{c}(s_0, t_0) = \text{cor}(Z(s_0, t_0), \mathbf{Z})$ .

Aryaputera et al. [2] used non-separable, direction dependent covariance models to forecast solar irradiance data.

- ▶ They used separate models fitted individually to time and space.
- ▶ The separate models were multiplied to make a separable covariance model.
- ▶ A non-separable model was used in which the separability parameterization of [3] was fitted.
- ▶ A directional model was used based on prior knowledge of wind for the day and location of their data set.

## Purpose

For this project, we introduce a visual method that uses the correlation in the irradiance data to specify the directional covariance model.

## Location Map

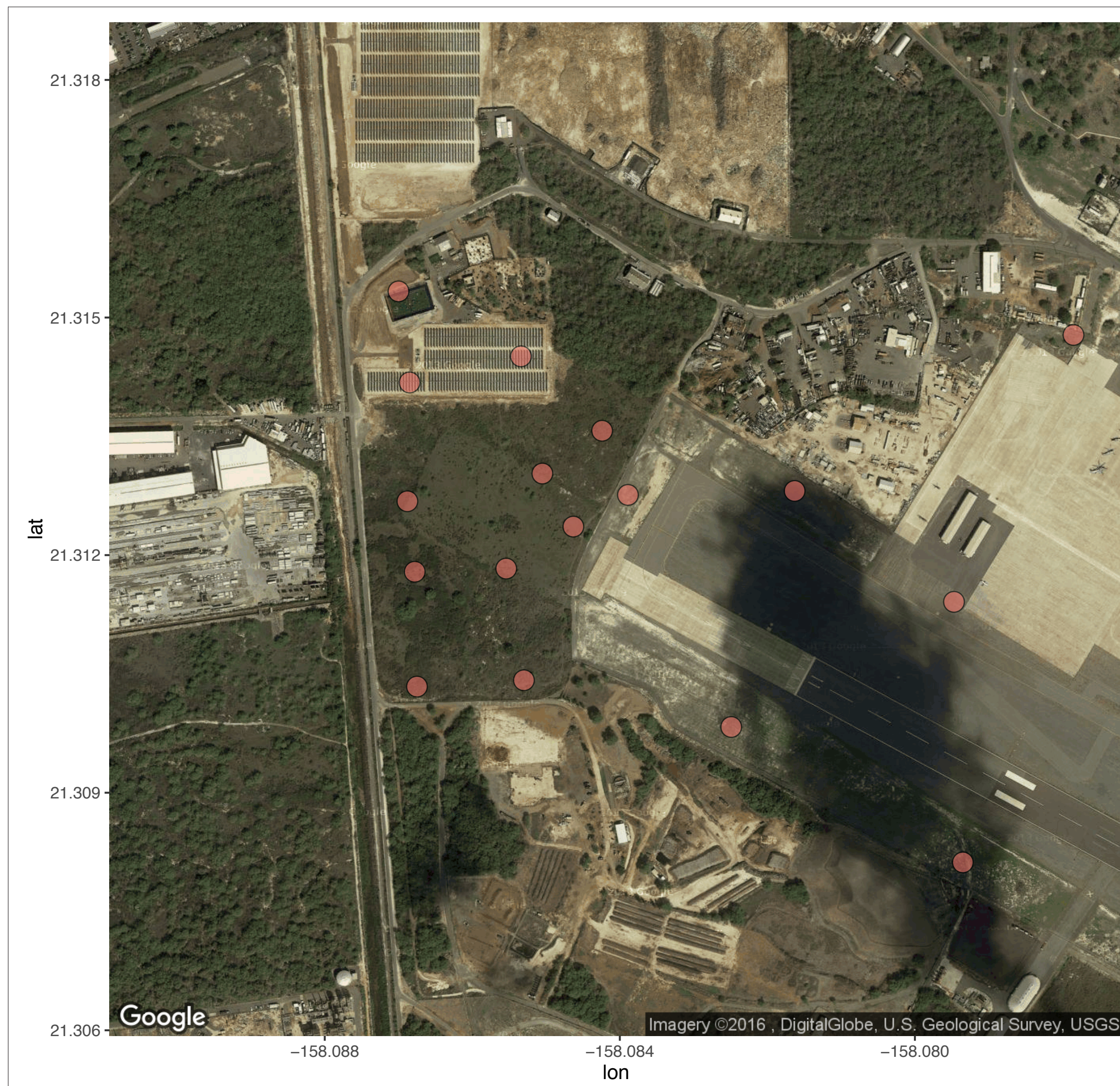


Figure: Oahu, Hawaii

The data come from 17 sensors placed at the Oahu, HI, airport. The data were obtained from the National Renewable Energy Laboratory (NREL). Irradiance measurements were taken once a second for the entire day of August 5, 2012. The data were then averaged over every 30 seconds with the measurements taken at night removed. A clear sky model was used to detrend the data [4].

## Separable and Fully Symmetric Models

- ▶ We first fit a separable covariance model by first fitting models to the spatial and time correlations separately:
- ▶ Exponential model for spatial:

$$C_s(\mathbf{h}) = (1 - \nu) \exp(-c\|\mathbf{h}\|) + \nu \mathcal{I}_{\mathbf{h}=0},$$

- ▶ Cauchy model for time:

$$C_t(u) = (a|u|^{2\alpha} + 1)^{-\tau}$$

- ▶ The separable covariance model is then

$$C_{sep}(\mathbf{h}, u) = C_s(\mathbf{h}) \times C_t(u)$$

- ▶ The non-separable fully symmetric model is

$$C_{FS}(\mathbf{h}; u) = \frac{1 - \nu}{(1 + a|u|^{2\alpha})} \times \left[ \exp\left(-\frac{c\|\mathbf{h}\|}{(1 + a|u|^{2\alpha})^{\frac{1}{2\alpha}}}\right) + \frac{\nu}{1 - \nu} \mathcal{I}_{\mathbf{h}=0} \right]$$

- ▶ The values of  $\nu$ ,  $c$ ,  $a$ , and  $\alpha$  are the same as for  $C_{sep}$ . Using these values,  $\beta$  is estimated which indicates the level of separability (0 = separable, 1 = non-separable).

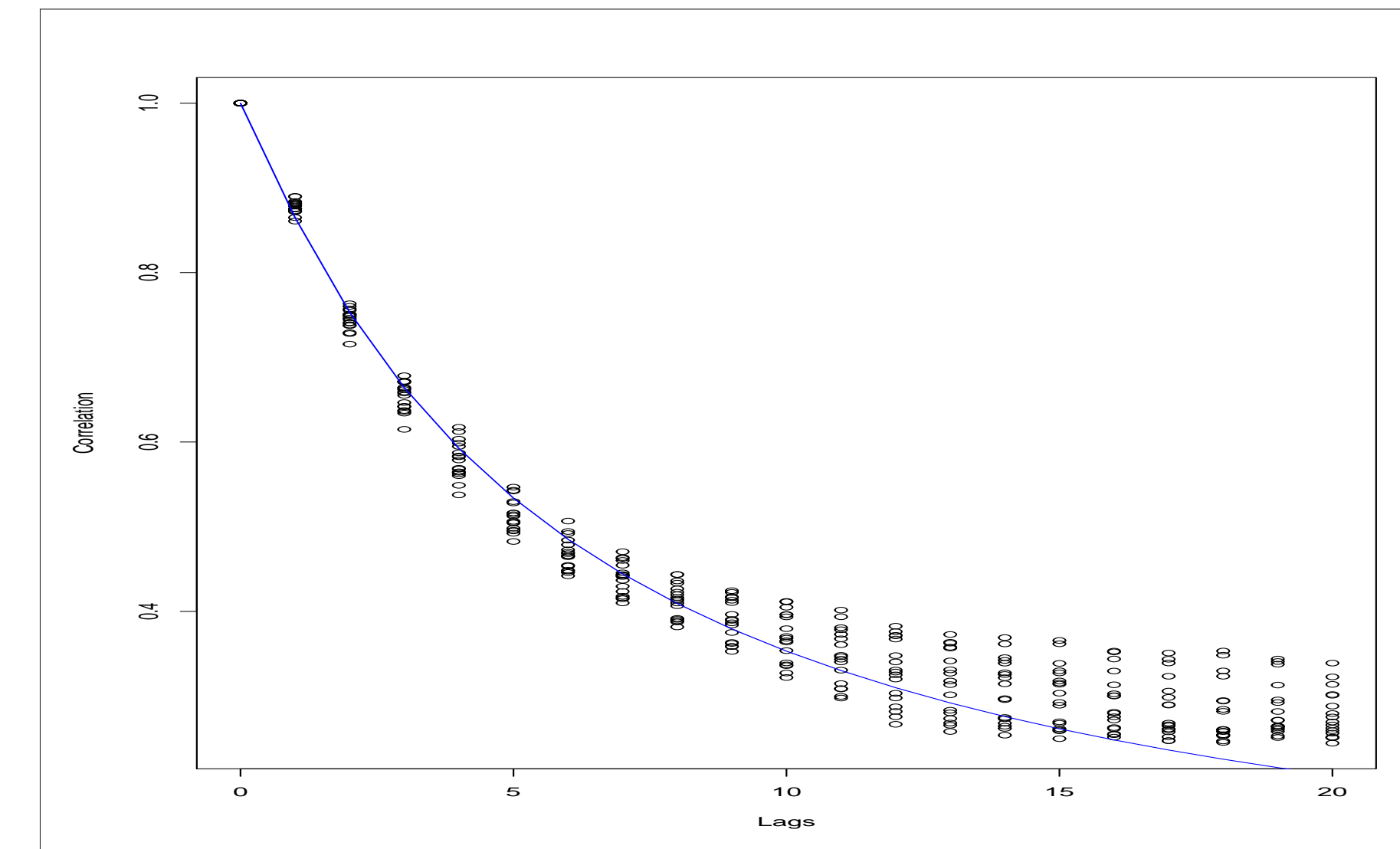


Figure: temporal-correlation

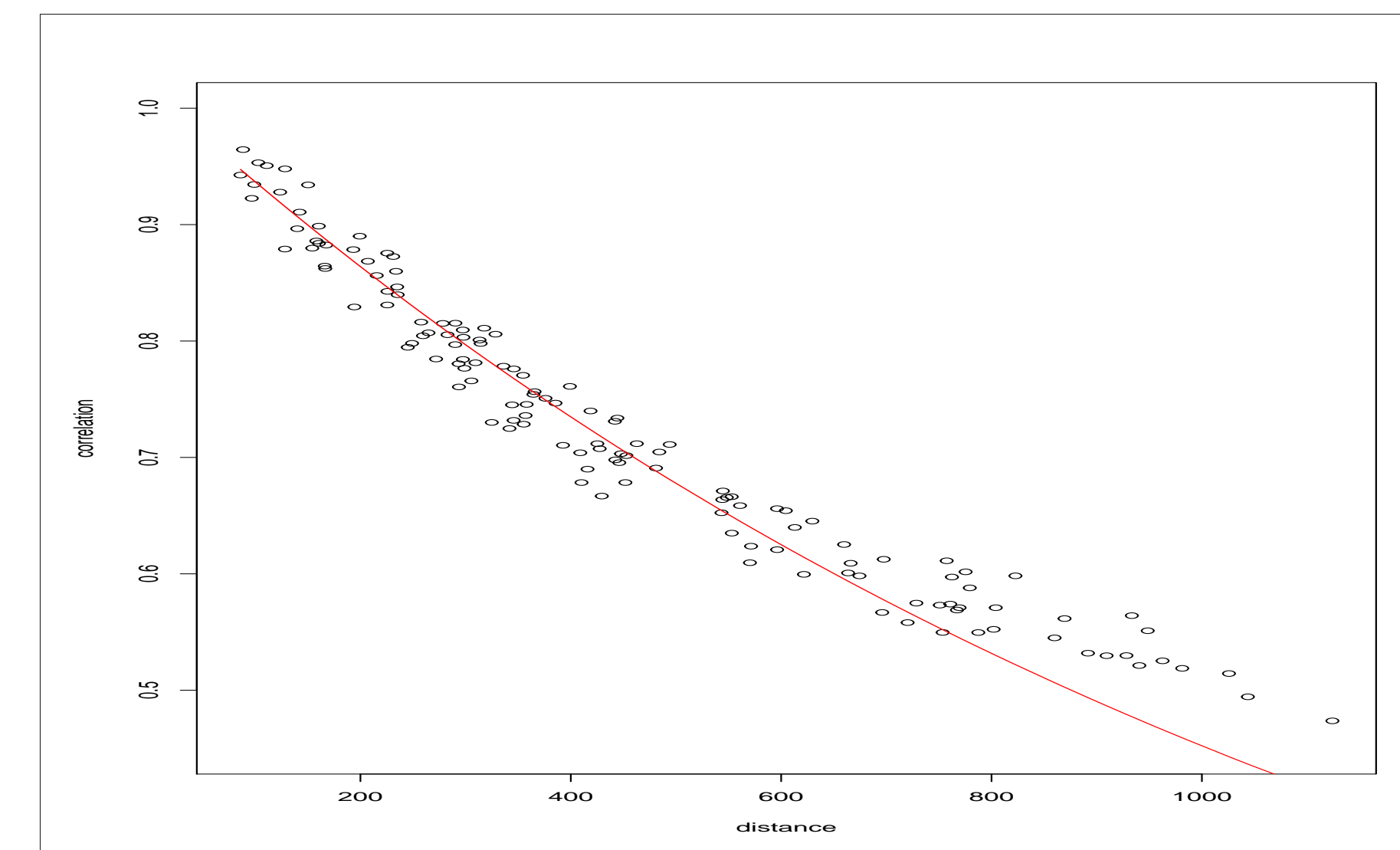


Figure: Spatial-correlation

## Directional Models

- ▶ Calculate the directional distances for each pair of sensors:  $h_1$  =along wind distance,  $h_2$  =crosswind distance
- ▶ Find the differences between along wind correlation,  $\text{corr}(Z(s_i, t - u), Z(s_j, t))$ , and against wind correlation,  $\text{corr}(Z(s_i, t), Z(s_j, t - u))$ , for some time lag  $u$  for each pair of sensors  $i \neq j$

- ▶ The difference correlation is modeled as

$$C_{diff}(\mathbf{h}, u) = \left( I_{u>0} I_{h_1>0} \left[ \beta_1^{(u)} h_1 + \beta_2^{(u)} h_2 + \beta_3^{(u)} h_1 h_2 + \beta_4^{(u)} h_1^2 + \beta_5^{(u)} h_2^2 \right] \right)_+$$

- ▶ The directional correlation function is then

$$C_{dir}(\mathbf{h}, u) = C_{FS}(\mathbf{h}, u) + \alpha C_{diff}(\mathbf{h}, u)$$

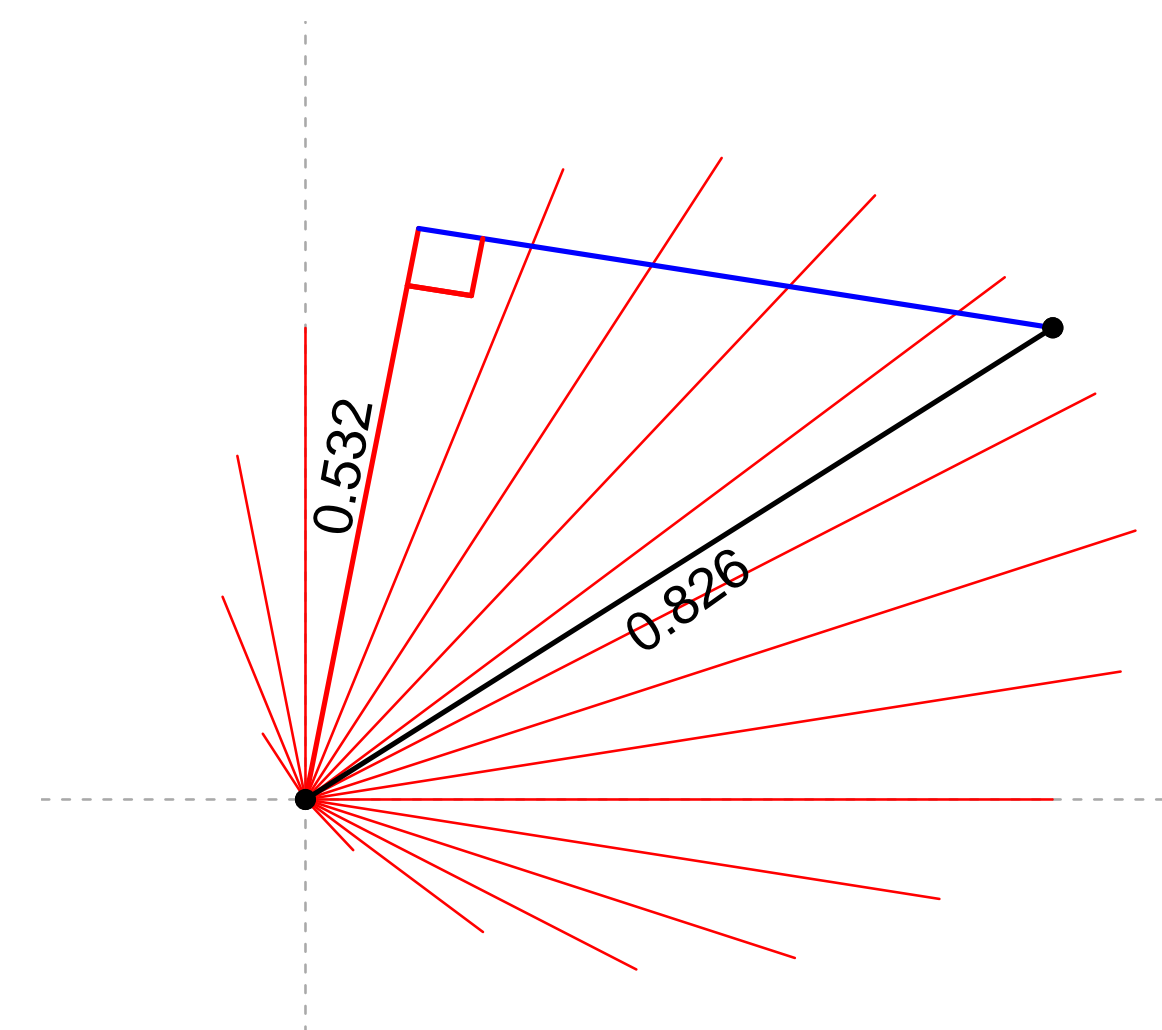


Figure: Example of directional distance

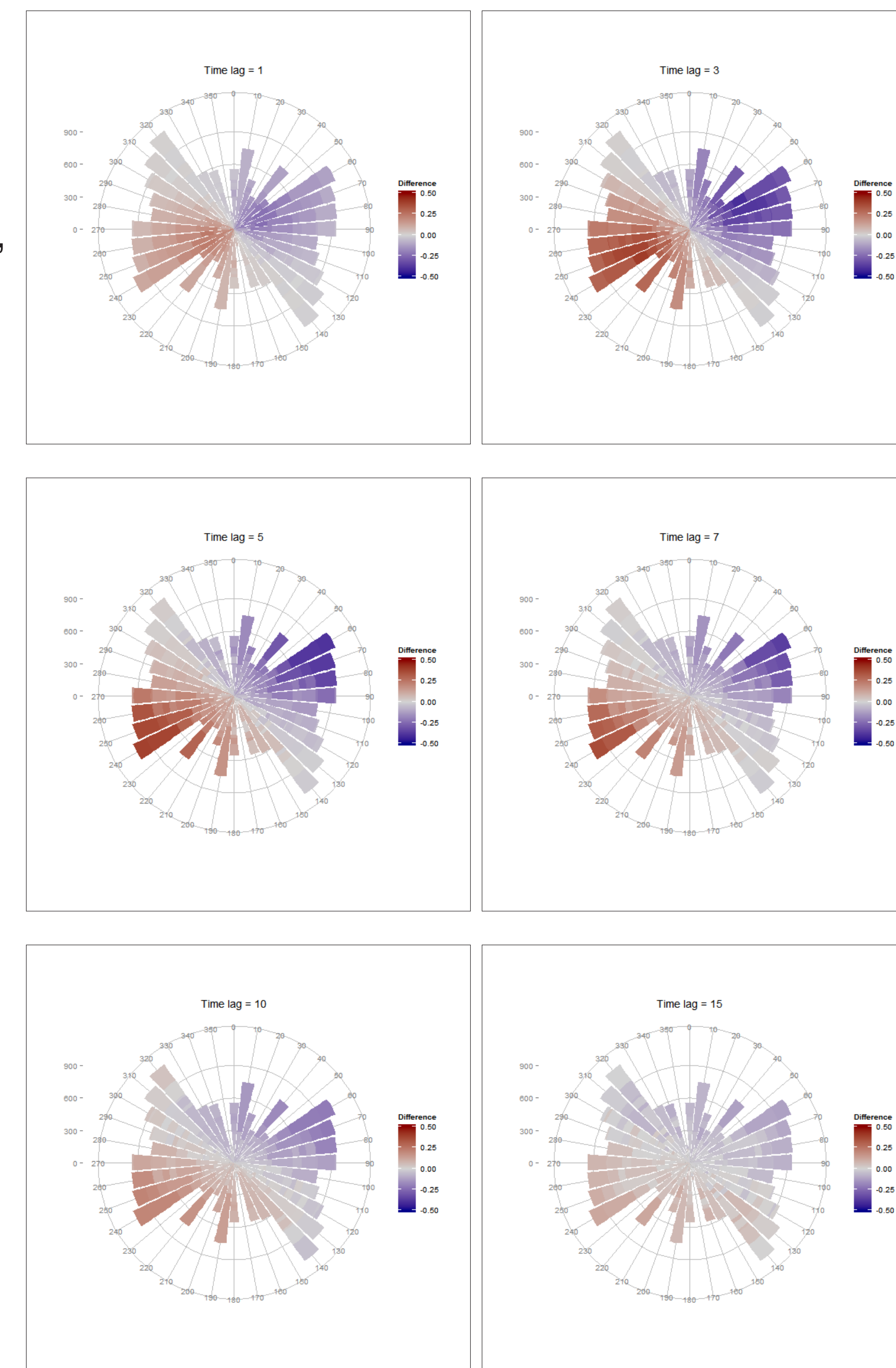


Figure: Directional correlation plots for the training data on Aug 5.

## Result

- ▶ We used 50% training data. We utilized a moving window approach in which the previous 50% data was used to fit the model and then predict the next  $u = 1, \dots, 10$  time points.
- ▶ Weighted nonlinear least squares implemented with the `nls` function in R were used to fit the Cauchy and exponential models to the time and spatial correlations, respectively. We used inverse distance weights.
- ▶ When determining the direction, we only examined directional plots for the first 50% training data. For computational speed, we did not regenerate for each predicted time point. Thus, we are assuming the wind direction stays constant throughout the day.
- ▶ From the directional plots, we determined that the previous 5 time points (2 and half minutes) of data should be used to predict the next time point(s).
- ▶ In the figure below, we can see that the directional model results in the lowest root mean squared prediction error.

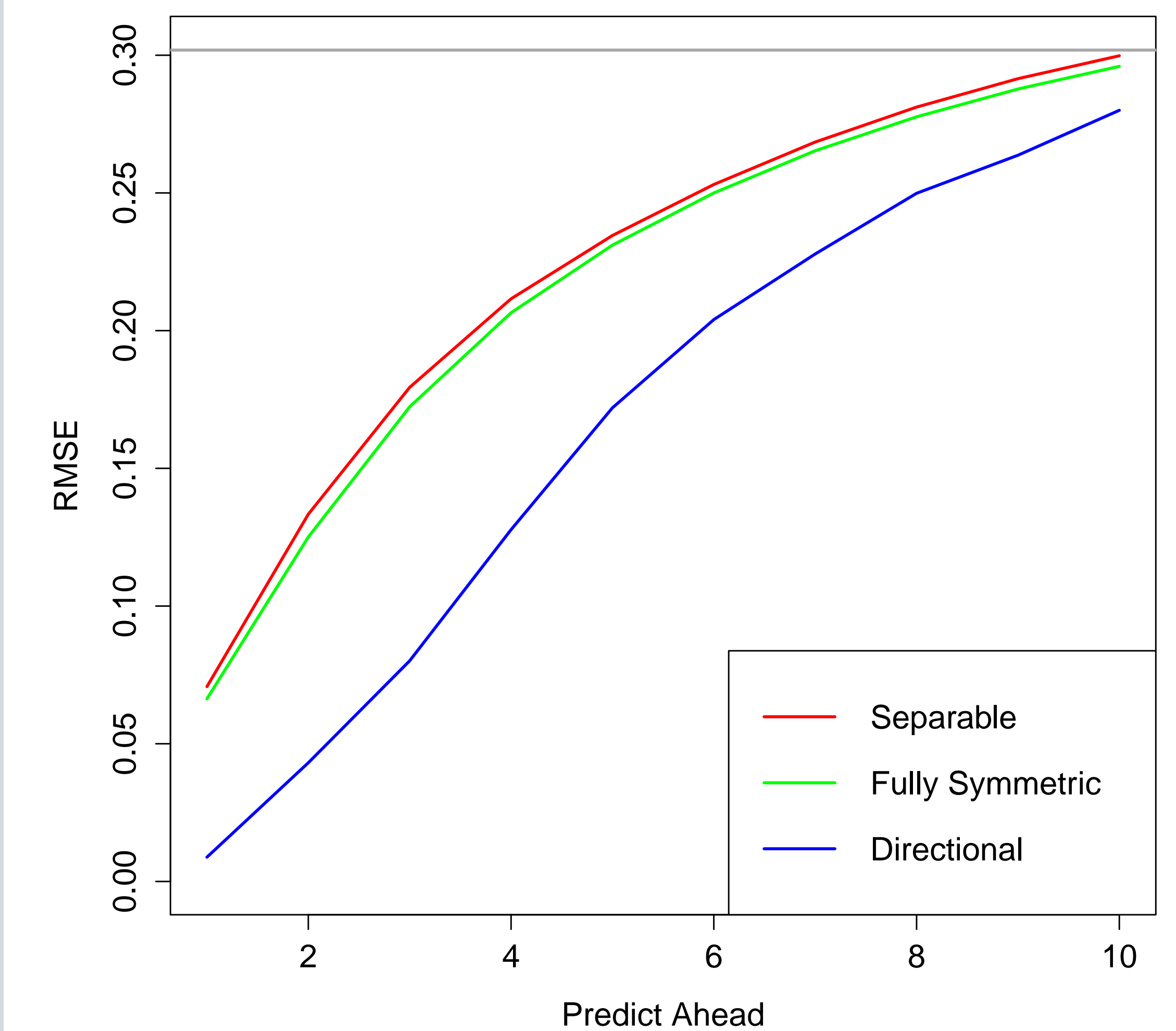


Figure: Root mean square prediction error for the three covariance models predicting 1, ..., 10 time points ahead. The gray line represents the standard deviation of the testing data.

## References

- [1] Noel Cressie and Hsin-Cheng Huang. Classes of nonseparable, spatio-temporal stationary covariance functions. *Journal of the American Statistical Association*, 94(448):1330–1339, 1999.
- [2] Aloysius W Aryaputera, Dazhi Yang, Lu Zhao, and Wilfred M Walsh. Very short-term irradiance forecasting at unobserved locations using spatio-temporal kriging. *Solar Energy*, 122:1266–1278, 2015.
- [3] Tilmann Gneiting, Marc G Genton, and Peter Guttorp. Geostatistical space-time models, stationarity, separability, and full symmetry. *Monographs On Statistics and Applied Probability*, 107:151, 2006.
- [4] Matthew J Reno, Clifford W Hansen, and Joshua S Stein. Global horizontal irradiance clear sky models: Implementation and analysis. *SANDIA report SAND2012-2389*, 2012.